This set of homework problems deals with perspective transformations, as well as transformation hierarchies.

**Problem 1: Perspective Transformation in 2D**

a) In class, we discussed that you need to specify the mapping of 5 points in general position to uniquely describe a 3D perspective transformation. How many points are required if we restrict ourselves to 2D?

b) Derive the $3 \times 3$ homogeneous matrix that maps the asymmetric view frustum drawn below into the square with corners at $(-1, -1)^T \ldots (1, 1)^T$.

![Perspective Transformation Diagram]

**Problem 2: Hierarchical Transformations**

Give an appropriate sequence of the following commands for drawing the scene depicted in the figure below. Assume that the current transformation matrix is initialized to the identity.

Commands (all transformation matrices are multiplied to current transformation matrix from the right):

- `drawSquare()`: draw a 1x1 square, bottom left corner at origin
- `translate(x, y)`: translation by x, y
- `scale(x, y)`: scaling in x and y direction
• `rotateZ(\text{theta})`: rotation around z axis (i.e. in x-y plane)
• `pushMatrix()`: duplicates top entry of matrix stack
• `popMatrix()`: deletes top entry of matrix stack